Assignment on Hotellings T^2

We consider two empirical dispersion matrices, each based on 10 observations

$$S_1 = \begin{bmatrix} 6 & -2 \\ -2 & 6 \end{bmatrix}$$
 and $S_2 = \begin{bmatrix} 4 & 2 \\ 2 & 4 \end{bmatrix}$

Furthermore we have the corresponding observed mean values

$$\bar{X} = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$$
 and $\bar{Y} = \begin{bmatrix} 6 \\ 6 \end{bmatrix}$

- 1. Find Hotellings T^2 based on the data above.
- 2. We assume that the underlying distributions for the X's and Y's in the two cases are the same. What is the probability of observing a more extreme value of T^2 than the one found in 1.?

kc fecit 24. Nov. 2012